



LOYOLA COLLEGE (AUTONOMOUS), CHENNAI – 600 034

B.Sc. DEGREE EXAMINATION – MATHEMATICS

FIRST SEMESTER – APRIL 2017

MT 1500- ALGEBRA, ANALY. GEO., CALCULUS & TRIGONOMETRY

Date: 26-04-2017
09:00-12:00

Dept. No.

Max. : 100 Marks

PART - A

Answer ALL the questions:

(10 X 2 = 20 Marks)

1. Find the n^{th} derivative of $y = \sin(ax + b)$.
2. Find the polar subtangent and polar subnormal of the curve $r = e^{\theta \cot \alpha}$.
3. Write the cartesian formula for the radius of curvature.
4. Define involute.
5. Find the equation, with rational coefficients one of whose roots is $\sqrt{5} + \sqrt{2}$
6. Calculate the sum of the cubes of the roots of the equation $x^4 + 2x + 3 = 0$
7. Show that $\cosh^2 x - \sinh^2 x = 1$
8. Write down the expansion for $\sin n\theta$.
9. Write the polar equation of a conic.
10. Find the asymptotes of the hyperbola $3x^2 - 5xy - 2y^2 + 17x + y + 14 = 0$

PART - B

Answer any FIVE questions:

(5 X 8 = 40 Marks)

11. Find the n^{th} differential coefficient of $\cos x \cdot \cos 2x \cdot \cos 3x$.
12. Find the slope of the tangent with the initial line for the cardioid $r = a(1 - \cos \theta)$ at $\theta = \frac{\pi}{6}$.
13. What is the radius of curvature of the curve $x^4 + y^4 = 2$ at the point (1,1) ?
14. The equation $x^3 - 3x + 1 = 0$ has a root between 1 and 2. Calculate it to three places of decimals by using Homer's method.
15. Express $\frac{\sin 6\theta}{\sin \theta}$ in terms of $\cos \theta$.
16. Separate into real and imaginary parts $\tan^{-1}(x + iy)$.
17. Derive the polar equation $\frac{l}{r} = 1 + e \cos \theta$ of a conic.
18. Show that in a conic the semi-latus rectum is the harmonic mean between the segments of a focal chord.

PART - C

Answer any TWO questions:

(2 x 20=40 Marks)

19. If $y = \sin(m \sin^{-1} x)$, prove that $(1 - x^2)y_2 - xy_1 + m^2y = 0$ and

$$(1 - x^2)y_{n+2} - (2n + 1)xy_{n+1} + (m^2 - n^2)y_n = 0$$

20. a) For the curves $x^2 = 4y$ and $y^2 = 4x$, find the angle of intersection. b) Prove

that the radius of curvature at any point of the cycloid

$$x = a(\theta + \sin\theta) \text{ and } y = a(1 - \cos\theta) \text{ is } 4a \cos \frac{\theta}{2}. \quad (12+8)$$

21. Solve the equation $81x^3 - 18x^2 - 36x + 8 = 0$ whose roots are in harmonic progression.

22. a) Sum to infinity the series $\cos\alpha + \frac{1}{2}\cos(\alpha + \beta) + \frac{1}{2} \cdot \frac{3}{4}\cos(\alpha + 2\beta) + \dots$

b) If e and e_1 are two extremities of hyperbola and its conjugate show that $e^{-2} + e_1^{-2} = 1$

(12+8)
