



Date: 30-04-2018

Dept. No. 

Max. : 100 Marks

Time: 01:00-04:00

**Part A (Answer ALL questions)**

( 10X2 = 20 )

1. Find the  $n^{\text{th}}$  derivative of  $y = \sin(ax + b)$ .
2. Show that in the parabola  $y^2 = 4ax$ , the subnormal is a constant.
3. Write the Cauchy's root test.
4. Find  $L^{-1}\left[\frac{1}{s(s-a)}\right]$
5. Find  $L(3t - 2e^{-2t})$ .
6. Define Skew-Hermitianmatrix and give an example.
7. Find the characteristics equation for the matrix  $A = \begin{bmatrix} 1 & 2 \\ -3 & 4 \end{bmatrix}$ .
8. Define rank correlation.
9. Write the expansion of  $(1-x)^{-4}$ .
10. Define binomial distribution.

**Part B (Answer any FIVE questions)**

( 5 x 8 = 40 )

11. Find the angle of intersection of the curves  $r = a(1+\cos\theta)$  and  $r = b(1-\cos\theta)$
12. Find the maximum and minimum value of the function  $f(x) = 2x^3 - 3x^2 - 36x + 10$ .

13. Find  $L[f(t)]$  if  $f(t) = \begin{cases} 0 & \text{if } 0 \leq t < 4 \\ t^2 & \text{if } 4 \leq t < 5 \\ 2t & \text{if } t \geq 5 \end{cases}$

14. Find  $L^{-1}\left[\frac{1}{s(s-1)(s-2)}\right]$

15. Solve the following system of equations using Crammer's rule

$$2x + 3y - z = 5$$

$$4x + 4y - 3z = 3$$

$$2x - 3y + 2z = 2$$

16. Test the convergence of the series  $\frac{1}{1.2.3} + \frac{3}{2.3.4} + \frac{5}{3.4.5} + \dots \infty$

17. Show that  $\log \sqrt{12} = 1 + \left(\frac{1}{2} + \frac{1}{3}\right)\frac{1}{4} + \left(\frac{1}{4} + \frac{1}{5}\right)\frac{1}{4^2} + \left(\frac{1}{6} + \frac{1}{7}\right)\frac{1}{4^3} + \dots$

18. Calculate the correlation coefficient for the following heights ( in inches ) of fathers (X) and their sons ( Y ).

X	65	66	67	67	68	69	70	72
Y	67	68	65	68	72	72	69	71

**Part C (Answer any TWO questions)**

( 2 x 20 = 40 )

19. a) If  $y = \sin(m \sin^{-1} x)$  prove that  $(1-x^2)y_{n+2} - (2n+1)xy_{n+1} + (m^2 - n^2)y_n = 0$

b) Find  $y_n$  if  $y = \frac{x^2}{(x-1)^2(x+2)}$

( 12 + 8 )

20. a) Using Laplace transform solve the differential equation  $\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + 5y = 4e^{-t}$  given  $y(0) = 0$  and  $y'(0) = 0$  using Laplace transform.

b) Evaluate  $L\left[\frac{1-e^{-t}}{t}\right]$

( 15 + 5 )

21.a) Find the Eigen values and Eigen vectors of the matrix  $A = \begin{bmatrix} 2 & 2 & 0 \\ 2 & 1 & 1 \\ -7 & 2 & -3 \end{bmatrix}$

b) Verify Cayley - Hamilton theorem and hence find the inverse of the matrix  $A = \begin{bmatrix} 7 & 3 \\ 2 & 6 \end{bmatrix}$

( 12 + 8 )

22. a) Find the sum of the series  $1 + \frac{1+3}{2!} + \frac{1+3+3^2}{3!} + \dots + \infty$

b) Calculate the mean and standard deviation for the following table giving the age distribution of 542 members.

<b>Age in years</b>	20 – 30	30 – 40	40 – 50	50 – 60	60 – 70	70 – 80	80 – 90
<b>Number of members</b>	3	61	132	153	140	51	2

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