LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600 034



B.Sc.DEGREE EXAMINATION - **MATHEMATICS**

SIXTH SEMESTER - APRIL 2019

MT 6607- DYNAMICS

Date: 05-04-2019	Dept. No.	Max. : 100 Marks
	<u> </u>	

Time: 09:00-12:00

SECTION - A

Answer ALL questions

 $(10 \times 2 = 20)$

- 1. State the principles of conservation of linear momentum.
- 2. State Newton's second law of motion.
- 3. Find the time taken by the particle to reach the maximum height in a projectile.
- 4. Define angle of Projection.
- 5. If T is the time of flight of the S.H.M., f its acceleration and v, velocity at any position, show that the expression $f^2T^2 + 4\pi^2v^2$ is a constant.
- 6. Define epoch.
- 7. Write down the differential equations of the central orbit of p-r co-ordinates.
- 8. Define apse.
- 9. Define moment of inertia.
- 10. What is the moment of inertia of circular ring of radius a about a tangent line.

SECTION - B

Answer any FIVE questions

(5x 8=40)

- 11. Show that when masses P and Q are connected by a string over the edge of a table, the tension is the same whether P hangs and Q is on the table or Q hangs and P is on the table.
- 12. A body, sliding down a smooth inclined plane, is observed to cover equal distances, each equal to a, in consecutive intervals of time t_1 , t_2 . Show that the inclination of plane to the horizon is $\sin^{-1}\left[\frac{2a(t_1-t_2)}{gt_1t_2(t_1+t_2)}\right]$.
- 13. State and prove perpendicular axes theorem.
- 14. A particle executing a S.H.M. in a straight line has velocities 8, 7, 4 at three distant one foot from each other. Find the period.
- 15. A particle moves in a simple harmonic motion in a straight line. In the first second, after starting from rest, it travels a distance a and in the next second, it travels a distance b in the same direction. Prove that the amplitude of the motion is $\frac{2a^2}{3a-b}$.
- 16. The velocities of a particle along and perpendicular to radius vector are radius radius vector
- 17. Obtain the differential equation of the central orbit.
- 18. Show that the Moment of inertia of a rectangular lamina.

SECTION - C

Answer any TWO questions

 $(2 \times 20 = 40)$

- 19. (i) Two particles of masses m_1 and m_2 ($m_1 > m_2$) are connected by means of a light inextensible string passing over a light, smooth fixed pulley. Discuss the motion.
 - (ii) A string passes over a fixed smooth pulley and to one end, there is attached a mass m_1 and to the other a smooth light pulley over which passes another string with masses m_2 and m_3 at the ends. If the system is released from rest. Show that m_1 will not move if $\frac{4}{m_1} = \frac{1}{m_2} + \frac{1}{m_3}$.

(10+10)

20. Show that the path of a projectile is a Parabola.

(20)

- 21. (i) Show that the resultant motion of two S.H.M of the same period in the same straight line.
 - (ii) If the law of acceleration is $5 \sim u^3 + 8 \sim c^2 u^5$ and the particle is projected from an apse at a distance c with a

velocity $\frac{3\sqrt{c}}{c}$. Prove that the equation of orbit is $r = c\cos\frac{2\pi}{3}$. (10+10)

- 22. (i) State and Prove Parallel axes theorem.
 - (ii) Find the moment of inertia of solid sphere about a tangent line. (10+10)
