LOYOLA COLLEGE (AUTONOMOUS), CHENNAI – 600 034



B.Sc. DEGREE EXAMINATION - **MATHEMATICS**

FIFTH SEMESTER - APRIL 2022

UMT 5602 - FUZZY SETS AND APPLICATIONS

Date: 21-06-2022	Dept. No.		Max. : 100 Marks
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Time: 09:00 AM - 12:00 NOON

Answer all Questions

PART – A

 $(10 \times 2 = 20)$

- 1. Define Fuzzy sets and give one example.
- 2. Define complement for the fuzzy subset and fine the complement for

$$A = \{(x_1, 1), (x_2, 0.8), (x_3, 0.2), (x_4, 0.8), (x_5, 0.6), (x_6, 0.3), (x_7, 0.5)\}$$

- 3. Define fuzzy relation with an example.
- 4. Write the symbols used for extrema (maxima & minima).
- 5. Define similitude relation.
- 6. Define fuzzy order relations.
- 7. Define limit cycle and a fixed point.
- 8. What is the difference between the FCM and the FRM model.
- 9. Define fuzzy control.
- 10. Define expert system.

Answer any 5 Questions

PART – B

 $(8 \times 5 = 40)$

11. Give the power set of the fuzzy subsets.

$$E = \{x_1, x_2\}, M = \{0, \frac{1}{2}, \frac{2}{3}, 1\}$$

12. Find the disjunctive sum for the following two fuzzy subsets

$$A = \{(x_1, 1), (x_2, 0.8), (x_3, 0.2), (x_4, 0.8), (x_5, 0.6), (x_6, 0.3), (x_7, 0.5)\}$$

$$B = \{(x_1, 0.8), (x_2, 0.3), (x_3, 0.6), (x_4, 0.5), (x_5, 0.4), (x_6, 0.7), (x_7, 0.6)\}$$

- 13. State and prove the decomposition theorem on fuzzy relations.
- 14. Considering the fuzzy similitude relation, R and choosing three quantities a, b, and c as the

following :
$$a = \mu_R(x, y) = \mu_R(y, x)$$
; $b = \mu_R(y, z) = \mu_R(z, y)$; $c = \mu_R(z, x) = \mu_R(x, z)$. Prove that $c \ge a = b$ or $a \ge c$ or $b \ge c = a$

- 15. Explain the following with an example.
 - a. Fuzzy order relation
 - b. Fuzzy relation of total order
 - c. Partially ordered fuzzy relations
- 16. Explain the concept used in FRM by taking a suitable example.
- 17. Using FCM analyze a social issue and give the conclusion
- 18. Explain the process of fuzzy control.

Answer any Two Questions

 $(2 \times 20 = 40)$

19. Let
$$A = \{(x_1, 1), (x_2, 0.8), (x_3, 0.2), (x_4, 0.8), (x_5, 0.6), (x_6, 0.3), (x_7, 0.5)\}$$

$$B = \{(x_1, 0.8), (x_2, 0.3), (x_3, 0.6), (x_4, 0.5), (x_5, 0.4), (x_6, 0.7), (x_7, 0.8)\}$$

$$C = \{(x_1, 0), (x_2, 0.5), (x_3, 0.2), (x_4, 0.7), (x_5, 0.6), (x_6, 0.9), (x_7, 0.1)\}$$

Calculate

i)
$$(\underline{A} \cup \underline{B}) \cap \underline{C}$$
 ii) $(\underline{A} \cap \underline{B}) \cup \underline{C}$ iii) $(\underline{A} \cap \underline{B}) \cup \underline{C}$ iv) $\underline{A} \cdot \underline{B} \cdot \underline{C}$
v) $\underline{A} + \underline{B} + \underline{C}$

20. a). Find $R_{1} \circ R_{2} \circ R_{3}$, where \circ is the max-min composition

$R_{_{\tilde{-}}}$ 1	Y_1	<i>Y</i> ₂	Y_3	Y_4	<i>Y</i> ₅
X_1	0.2	0.3	0.8	0.6	0.1
	0.3	0.8	0.6	0.6	1
X_3	0.2	1	0.4	0.1	0

$R_{_{\tilde{a}}}$ 2	Z_1	Z_2	Z_3	Z_4
Y_1	1	0.2	0.3	0.4
Y_2	0.4	1	0.1	0.2
<i>Y</i> ₃	0.3	0.4	1	0.1
Y_4	0.2	0.3	0.4	1
<i>Y</i> ₅	1	0.2	0.3	0.4

$R_{_{_{\sim}}}3$	T_1	T_2	T_3	T_4	T_5
Z_1	0.9	0	0.3	0.4	0.5
	0.9	0.6	0.4	0.7	0.6
Z_3	0	0.8	0.9	0.3	0.7
Z_4	0.3	1	0.1	0.4	1

(12 Marks)

b). Consider the relation R given by

$R_{\tilde{x}}$	A	В	С
A	1	0.1	0.8
В	0.1	1	0
C	0.8	0	1

- i). Show that R is a resemblance relation
- ii). Find the min-max distance in the resemblance relation.

(8 Marks)

- 21. Use FAM model to study the social economic problem of women with HIA/AIDS and give the prediction.
- 22. a). Write the characteristics attributes of an expert system.

(10 Marks)

b). Explain the structure of an expert system.

(10 Marks)