## LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034

## M.Sc. DEGREE EXAMINATION - PHYSICS <br> FIRST SEMESTER - APRIL 2023 <br> PPH1MC01 - CLASSICAL MECHANICS

Date: 29-04-2023
Time: 09:00 AM - 12:00 NOON
Max. : 100 Marks

| SECTION A |  |  |  |
| :---: | :---: | :---: | :---: |
| Answer ALL the questions |  |  |  |
| 1 | Answer the following | ( $5 \times 1=5$ ) |  |
| a) | When a horse pulls a cart, which is the force that helps the horse to move forward? | K1 | CO1 |
| b) | Define configuration space. | K1 | CO1 |
| c) | What are generalised co-ordinates? | K1 | CO1 |
| d) | Write down Hamilton- Jacobi equation. | K1 | CO1 |
| e) | If a lighter object and a heavier object have the same kinetic energy, which one will have the greater momentum? | K1 | CO1 |
| 2 | Answer the following | ( $5 \times 1=5$ ) |  |
| a) | Check whether the force $\mathbf{F}=\mathrm{x}^{2} \mathrm{yzi}-\mathrm{xyz}^{2} \mathbf{k}$ is conservative or non-conservative. | K2 | CO1 |
| b) | What is Inertia tensor? | K2 | CO1 |
| c) | Show that the work done by force of constraint in a rigid body is zero. | K2 | CO1 |
| d) | With examples, classify constraints. | K2 | CO1 |
| e) | State the conservation theorem for angular momentum for a system of N-particles. | K2 | CO1 |
| SECTION B |  |  |  |
|  | Answer any THREE of the following in 500 words | $(3 \times 10=30)$ |  |
| 3 | State D'Alembert's principle. What is its importance? | K3 | CO3 |
| 4 | Explain the terms :Normal frequencies, Normal modes of vibrations and Normal co ordinates of a coupled system. | K3 | CO3 |
| 5 | Prove that $[\mathrm{F}+\mathrm{K}, \mathrm{G}]=[\mathrm{F}, \mathrm{G}]+[\mathrm{K}, \mathrm{G}]$. | K3 | CO3 |
| 6 | The moment of inertia is the rotational analogue of mass of a body, Explain. | K3 | CO 3 |
| 7 | Using Hamilton's canonical equations, derive the equation of motion of a particle moving in a force field in which the potential is given by $V=-k / r$, where $k$ is positive. | K3 | CO3 |
| SECTION C |  |  |  |
| Answer any TWO of the following in 500 words $\quad(2 \times 12.5=25)$ |  |  |  |
| 8 | The Lagrangian of a system in terms of generalised co-ordinates x and y is given by $L=\dot{x} \dot{y}-x y$. Find Lagrangian equations of motion. | K4 | CO3 |
| 9 | Discuss the problem of scattering of a charged particle by a coulomb field and obtain Rutherford formula for scattering cross section. | K4 | CO3 |
| 10 | Describe any two applications of Legendre transformation in mechanics. | K4 | CO3 |
| 11 | Discuss in detail the vibrations of a linear triatomic molecule. | K4 | CO3 |

## SECTION D

## Answer any ONE of the following in 1000 words

Show that the K.E. of a rotating rigid body in a co-ordinate system of principal axes is given by $T=1 / 2\left(I_{1} \omega_{1}{ }^{2}+I_{2} \omega_{2}{ }^{2}+I_{3} \omega_{3}{ }^{2}\right)$

When is Hamilton -Jacobi theory useful? Discuss the harmonic oscillator problem using Hamilton-Jacobi method.

## SECTION E

Answer any ONE of the following in $\mathbf{1 0 0 0}$ words

What is Hamilton's principle? Derive Lagrange's equation from Hamilton's principle for a conservative system. Derive equation of motion for a particle moving under a central force.

Consider the case of two coupled pendulums. Determine
a. T and V matrices.
b. The normal frequencies.

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c. The normal co-ordinates.

K6
CO 5
d. The equation of motion.
e. The eigen-vectors.
f. The general solution.

