## LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034

B.B.A.DEGREE EXAMINATION -BUSINESS ADMINISTRATION

FOURTH SEMESTER - APRIL 2018
16UBU4MC01- ELEMENTS OF OPERATIONS RESEARCH

Date: 20-04-2018
Time: 09:00-12:00

## Dept. No.

$\square$ Max. : 100 Marks

## Answer ALL the questions:

(10 X 2=20)

1. What is operations research?
2. Explain any two features of Operations research.
3. Explain any two applications of LPP in Management.
4. What do you mean by Feasible Solution?
5. Develop a Linear programming model to determine the optimal production volume of each of the products such that the profit is maximised subject to the availability of machine hours.

|  | Processing Time <br> (Hours) |  |  |
| :---: | :---: | :---: | :---: |
| Machine Type | Product <br> P1 | Product <br> P2 | Machine Hour <br> Available per <br> week |
| Milling Machine | 2 | 5 | 200 |
| Drilling Machine | 4 | 2 | 160 |
| Profit/unit (₹ ) | 250 | 400 |  |

6. Determine the optimal strategy/strategies for Company A and Company B.

|  |  | Company B |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ |
| Company <br> $\mathbf{A}$ | $\mathbf{1}$ | 20 | 15 | 22 |
|  | $\mathbf{2}$ | 35 | 45 | 40 |
|  | $\mathbf{3}$ | 18 | 20 | 25 |

7. Reduce the 3 X 3 Matrix to 2 X 2 Matrixes.

|  |  | Player B |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ |
| Player A | $\mathbf{1}$ | 20 | -20 | 50 |
|  | $\mathbf{2}$ | -25 | 25 | -25 |
|  | $\mathbf{3}$ | 20 | -50 | 50 |

8. Explain the concept Dominance property.
9. What do you mean by Assignment Problem?
10. Explain Balanced Transportation Problem.

## PART - B

## Answer any FOUR Questions:

$(4 X 10=40)$
11. What are the advantages and limitations of LP problem?
12. A firm manufactures two types of products A and B and sells them at a profit of 4 on type A and 6 on type B. Each product is processed on two machines G and H. Type A requires 2 minutes of processing time on $G$ and 4 minutes on $H$, type $B$ requires 2 minutes on $G$ and 2 minute on $H$. The machine $G$ is available for not more than 6 hours 40 minutes while machine H is available for 10 hours during any working day. Formulate the problem as a LPP.
13. Use graphical method to solve the following LP Problem.

Maximize $Z=3 x+5 y$

$$
\begin{aligned}
& \qquad \begin{aligned}
& \text { Subject to } x+2 y \leq 2000 \\
& x+y \leq 1500 \\
& y \leq 600
\end{aligned} \\
& \text { and } x, y \geq 0
\end{aligned}
$$

14. A company has factories which supply warehouses. Unit shipping costs (in rupees) are as follows:

|  | Warehouse |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  | W1 | W2 | W3 | Supply |
| Factory | F1 | 16 | 20 | 12 | 200 |
|  | F2 | 14 | 8 | 18 | 160 |
|  | F3 | 26 | 24 | 16 | 90 |
|  | Demand | 180 | 120 | 150 | 450 |

Determine the optimum distribution for this company to minimise shipping costs using Least Cost Cell Method:
15. The departmental head has four task and four subordinates to be performed. The subordinates differ in efficiency and the tasks differ in their intrinsic difficulty. His estimates of the time each man would take to perform each task is given below in the matrix:

|  | Tasks |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Subordinates | I | II | III | IV |
| A | 8 | 26 | 17 | 11 |
| B | 13 | 28 | 4 | 26 |
| C | 38 | 19 | 18 | 15 |
| D | 19 | 26 | 24 | 10 |

16. Consider the 4 X 4 game which represents the payoff matrix of Player A and solve it optimally:

|  | Player B |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- |
| Player |  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
|  | A | $\mathbf{1}$ | 3 | 2 | 4 |
|  | $\mathbf{2}$ | 3 | 4 | 2 | 4 |
|  | $\mathbf{3}$ | 4 | 2 | 4 | 1 |
|  | $\mathbf{4}$ | 3 | 4 | 3 | 4 |

17. Consider the payoff matrix of Player A and solve it optimally using graphical method:

|  |  | Player B |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |  |
| Player A | $\mathbf{1}$ | 3 | 0 | 6 | -1 | 7 |  |
|  | $\mathbf{2}$ | -1 | 5 | -2 | 2 | 1 |  |

## PART - C

Answer any TWO Questions: (2 X $20=40$ )
18. Briefly explain the limitations of game theory and its types.
19. Use simplex method to solve the LPP

$$
\begin{aligned}
& \text { Maximize } Z=4 \mathrm{x} 1+10 \mathrm{x} 2 \\
& \text { Subject to } \quad 2 \mathrm{x} 1+\mathrm{x} 2 \leq 50 \\
& 2 \mathrm{x} 1+5 \mathrm{x} 2 \leq 100 \\
& 2 \mathrm{x} 1+3 \mathrm{x} 2 \leq 90 \\
& \text { and } \mathrm{x} 1, \mathrm{x} 2 \geq 0
\end{aligned}
$$

20. Certain equipment needs five repair jobs which have to be assigned to five machines. The estimated time (in hours) that each mechanic requires to complete the repair job is given in the following table:

|  | Jobs |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Machines | J1 | J2 | J3 | J4 | J5 |
| M1 | 7 | 5 | 9 | 8 | 11 |
| M2 | 9 | 12 | 7 | 11 | 10 |
| M3 | 8 | 5 | 4 | 6 | 9 |
| M4 | 7 | 3 | 6 | 9 | 5 |
| M5 | 4 | 6 | 7 | 5 | 11 |

21. A company has factories which supply warehouses. Unit shipping costs (in rupees) are as follows:

| Plant | Market |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | M1 | M2 | M3 | M4 | M5 |  |
| P1 | 10 | 2 | 16 | 14 | 10 | 300 |
| P2 | 6 | 18 | 12 | 13 | 16 | 500 |
| P3 | 8 | 4 | 14 | 12 | 10 | 825 |
| P4 | 14 | 22 | 20 | 8 | 18 | 375 |
| Demand | 350 | 400 | 250 | 150 | 400 |  |

Find the initial basic feasible solution using VAM.

