Date: 02-05-2017
Time: 01:00-04:00

Dept. No.
Max. : 100 Marks

## PART-A

Answer all the questions: -
$10 X 2=20$

1. Define Minor of a matrix.
2. Obtain the Characteristic equation of $\left[\begin{array}{cc}1 & -2 \\ -5 & 4\end{array}\right]$
3. The following are the sizes of the last 8 dresses sold at a women's boutique:
$8,10,6,4,10,12,14,10$. What is the sample mode?
4. Listthe properties of the sample correlation coefficient.
5. Draw Petersen graph.
6. Define Isomorphism graph.
7. Draw a tree with 6 vertices.
8. Define Trail?
9. State the order of convergence of Neuton Raphson method.
10. Write the formula for false position method.

## PART-B

$5 \times 8=40$
Answer all the Questions:-
11. a) Test whether the following system of equation is consistent or not.

$$
\begin{gathered}
x-y+z=-9, \quad 2 x-y+z=4,3 x-y+z=6,4 x-y-2 z=7 \\
\text { Or }
\end{gathered}
$$

b) Find the Eigen values and Eigen vectors of the matrix $A=\left[\begin{array}{ll}4 & 1 \\ 3 & 2\end{array}\right]$
12. Consider five numbers. Suppose the mean of the first four numbers is 14.
a) i)If the fifth number is 24 , what is the mean of all five numbers?
ii) If the mean of all five numbers is 24 , what is the fifth number?

## Or

b)The following data give the yearly numbers of law enforcement officers killedin the United States over 10 years:
$164,165,157,164,152,147,148,131,147,155$.Find the sample variance of the number killed in these years.
13. a) Prove that any self-complementary graph has $4 n$ or $4 n+1$ points.

## Or

b)Prove that i) $\delta \leq \frac{2 q}{p} \leq \Delta$
ii)Show that the partition $\mathrm{P}=(6,6,4,5,3,3,1)$ is not graphic.
14. a)Show that every non-trivial tree G has at least two vertices of degree 1

Or
b) Write short note on following.
(i) Eulerian graph
(ii) Konigsberg bridge problem.
(iii) Hamiltonian graph.
15. a)Using Newton's iterative method find the positive root between 0 and 1 of $x^{3}=6 x-4$ Correct to two decimal places.

Or
b) Evaluate $\int_{0}^{1} \frac{d x}{1+x^{2}}$ with $\mathrm{h}=1$ by Trapezoidal rule 6

## PART-C

Answer Any TWO Questions 2X20=40

16 a) If $\mathrm{A}=\left(\begin{array}{lll}1 & 0 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0\end{array}\right)$ Find its inverse and $\boldsymbol{A}^{4}$ using Cayley Hamilton theorem.
c) Compute the sample correlation coefficient of the data of Table, whichrelates the number of cigarettes smoked to the number of free radicals foundin a person's lungs.
Cigarette Smoking and Free Radicals
Person Number of cigarettes smokedFree radicals

| 1 | 18 | 202 |
| :--- | :--- | :--- |
| 2 | 32 | 644 |
| 3 | 25 | 411 |
| 4 | 60 | 755 |
| 5 | 12 | 144 |
| 6 | 25 | 302 |
| 7 | 50 | 512 |
| 8 | 15 | 223 |
| 9 | 22 | 183 |
| 10 | 30 | 375 |

17a)Prove the following statement. The maximum number of lines among all p point graphs with no triangles is $\left[p^{2} / 4\right]$
d) (I) Define Tree
(ii) Write the characteristics of trees.
e) Prove that every connected graph has a spanning tree.

18 a)Evaluate $\int_{0}^{6} \frac{d x}{1+x^{2}}$ using (i)Simpson's $1 / 3^{\text {rd }}$ rule(ii) Simpson's $3 / 8^{\text {th }}$ rule

$$
\text { f) If } y(10)=35.3, y(15)=32.4, y(20)=29.2, y(25)=26.1, y(30)=23.2, y(35)=20.5 \text { find } y(12)
$$

using (i) Newton's forward interpolation formula.
(ii)Newton's backward interpolation formula.

