## M.A.DEGREE EXAMINATION - ECONOMICS

FIRSTSEMESTER - NOVEMBER 2017

## EC 1809- MATHS \& STATISTICS FOR ECONOMISTS

$\square$

## PART - A

Answer any FIVE questions in about 75 words each

1. Distinguish between Type I and Type II errors.
2. State the properties of a good estimator.
3. Using scatter diagrams represent perfect positive correlation and perfect negative correlation.
4. Find the characteristic roots of the matrix $\mathrm{A}=\left[\begin{array}{cc}10 & 3 \\ 3 & 2\end{array}\right]$
5. Find $\frac{\partial z}{\partial x}$ and $\frac{\partial z}{\partial y}$ for $\mathrm{Z}=12-\mathrm{x}^{2}-\mathrm{y}^{2}+\mathrm{xy}$
6. Find $2 \mathrm{~A}-3 \mathrm{~B}$

$$
A=\left[\begin{array}{ll}
1 & 2 \\
3 & 4
\end{array}\right] \quad B=\left[\begin{array}{cc}
-1 & 2 \\
2 & -1
\end{array}\right]
$$

7. Find $|A|$ given $\mathrm{A}=\left[\begin{array}{lll}3 & 4 & 7 \\ 2 & 1 & 3 \\ 7 & 2 & 1\end{array}\right]$

## PART - B

Answer any FOUR questions in about 300 words each $\quad(4 \times 10=40)$
8. Solve the following set of simultaneous linear equations using Cramer's rule

$$
\begin{gathered}
3 x_{1}+x_{2}-x_{3}=2 \\
x_{1}-2 x_{2}+x_{3}=-9 \\
4 x_{1}+3 x_{2}+2 x_{3}=1
\end{gathered}
$$

9. Elucidate the procedure for testing hypothesis.
10. Two ladies were asked to rank 7 different types of lipsticks. The ranks given by them are as follows:

Lipsticks: A B C D E F
Neelu : $\begin{array}{llllllll}2 & 1 & 4 & 3 & 5 & 7 & 6\end{array}$
Meena : $\begin{array}{llllllll}1 & 3 & 2 & 4 & 5 & 6 & 7\end{array}$
Calculate Spearman's rank correlation coefficient.
11. Examine the function $f(x, y)=x^{2}+x y+y^{2}-3 x+2$ for maximum and minimum values.
12. Find the inverse of $\left[\begin{array}{lll}1 & 4 & 3 \\ 4 & 2 & 1 \\ 3 & 2 & 2\end{array}\right]$
13. Explain the practical uses of Poisson distribution.
14. Given $Z=x^{2}-2 x y+y^{2}$, find the first and second order total differentials.

## PART - C

## Answer any TWO questions in about 1200 words each $\quad(2 \times 20=40)$

15. Solve the following input-output model using Leontief inverse and find the gross output of the economy
P $\quad$ Q R
$\mathrm{A}=\left[\begin{array}{ccc}0.3 & 0.5 & 0.2 \\ 0.2 & 0 & 0.5 \\ 0.1 & 0.3 & 0.1\end{array}\right] \quad \mathrm{F}=\left[\begin{array}{c}100 \\ 40 \\ 50\end{array}\right]$
16. 

a) Explain the uses of $\chi^{2}$ estimates.
b) From the data given below about the treatment of 250 patients suffering from a disease, state whether the new treatment is superior to the conventional treatment.

| Treatment | No. of Patients |  |  |
| :--- | :---: | :---: | :---: |
|  | Favourable | Non-favourable | Total |
| New | 140 | 30 | 170 |
| Conventional | 60 | 20 | 80 |
| Total | 200 | 50 | 250 |

$\left(\right.$ Given for degree of freedom $=1, \chi^{2}$ at $5 \%=3.84$ )
17. Consider the following data:

Marks in Economics : $\begin{array}{llllllllll}25 & 28 & 35 & 32 & 31 & 36 & 29 & 38 & 34 & 32\end{array}$
Marks in Statistics : $\begin{array}{lllllllllll}43 & 46 & 49 & 41 & 36 & 32 & 31 & 30 & 33 & 39\end{array}$
a) Find the regression equations ' X on Y ' and ' Y on X '.
b) Find the correlation between marks in Economics and Statistics.
c) The most likely marks in Statistics when the mark in Economics is 30 .
18. Determine the maxima or minima of the function $f\left(x_{1}, x_{2}, x_{3}\right)=x_{1}{ }^{2}+2 x_{2}{ }^{2}+x_{3}{ }^{2}+x_{1} x_{2}-2 x_{3}-7 x_{1}+$ 12.

