LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034
B.Sc. DEGREE EXAMINATION - STATISTICS

FIFTH SEMESTER - NOVEMBER 2017
ST 5507/ST 5503-COMPUTATIONAL STATISTICS

Date: 10-11-2017
Dept. No. $\square$ Max. : 100 Marks

## ANSWER ANY THREE QUESTIONS:

1 a) Obtain the equation of the normal curve that may be fitted to the following data:

| class | $60-65$ | $65-70$ | $70-75$ | $75-80$ | $80-85$ | $85-90$ | $90-95$ | $95-100$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| frequency | 3 | 21 | 150 | 335 | 326 | 135 | 26 | 4 |

Obtain the expected normal frequencies and test the goodness of fit.
b) A firm that runs a string of retail outlets across a city receives complaints from its clients regarding quality and other aspects and maintains a register of complaints. The following are data on the number of complaint sreceived on100 randomly chosen days:

| No. of Complaints | 0 | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| No. Of day | 30 | 25 | 20 | 18 | 7 |

Test at $5 \%$ level of significance whether the number of complaints per day follows Poisson distribution.
a) Two horses A and B were tested according to the time (in seconds) to run a particular distances with the following results:

| Horse A | 30 | 32 | 34 | 35 | 36 | 31 | 37 | 38 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Horse B | 31 | 33 | 31 | 2 | 28 | 32 | 35 |  |

Test whether the two horses have the same running capacity. Use 5\% significance level.
b) Obtain $90 \%$ Confidence interval for the mean of the normal population. The data are given below.

| 10 | 6 | 16 | 17 | 13 | 12 | 8 | 14 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | 9 | 7 | 13 | 22 | 15 | 12 | 14 |
| 18 | 8 | 21 | 23 | 10 | 17 | 25 | 18 |
| 12 | 19 | 27 | 34 | 39 | 23 | 11 | 24 |

c) In a sample of 650 men from a large city, 400 are found to be smokers. In another city 500 out of 900 are found to be smokers. Test whether the cities are significantly different with respect to smoking habit.
a) A population with 300 units is divided into three strata. A stratified random sample was drawn and the observed values in the sample are reported below:

| Stratum No. | Stratum Size | Sample observations |
| :---: | :---: | :---: |
| 1 |  |  |
| 2 | 80 | 21,25 |
| 3 | 100 | $32,35,40$ |

Obtain the estimate and get an estimate of its variance from the sample data.
b) Construct a sampling distribution of the sample mean for the following population when random sample of size 2 are taken from it (a) with replacement and (b) without replacement. Also find mean and standard error of the distribution in each case.

| Population Unit | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| observation | 22 | 24 | 26 | 28 |

a) Calculate the 4 yearly moving averages and 5 yearly moving averages of the following data. Obtain trend values and give their graphical representation.

| year | Output (in 1000's) | year | Output (in 1000's) |
| :---: | :---: | :---: | :---: |
| 1990 | 4 | 1998 | 8 |
| 1991 | 5 | 1999 | 7 |
| 1992 | 6 | 2000 | 6 |
| 1993 | 7 | 2001 | 8 |
| 1994 | 9 | 2002 | 9 |
| 1995 | 6 | 2003 | 10 |
| 1996 | 5 | 2004 | 7 |
| 1997 | 7 | 2005 | 9 |

b) Compute index number for the given data using the following methods (i) Laspeyre's method (ii) Passche's method and (iii) Fisher's ideal formula

| Items | Base Year |  | Current Year |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Prices (Rs) | Expenditure | Prices (Rs) | Expenditure |
| A | 6 | 360 | 10 | 460 |
| B | 2 | 240 | 4 | 240 |
| C | 4 | 350 | 6 | 360 |
| D | 10 | 240 | 12 | 360 |
| E | 8 | 320 | 12 | 432 |

c) Construct index number by chain base method from the following data of wholesale prices of a certain commodity:

| Year | 2000 | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Price | 75 | 50 | 65 | 60 | 72 | 70 | 69 | 75 | 84 | 80 |

5 a) Use Wilcoxon Signed rank test to see if there is a difference between the number of days until collection of an account receivable before and after a new collection policy. Use the $5 \%$ level of significance.

| Before | 30 | 28 | 40 | 42 | 34 | 28 | 27 | 25 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| After | 32 | 29 | 37 | 43 | 37 | 27 | 33 | 30 |

b) Test for randomness for the following data based on run test:

| 15 | 77 | 01 | 65 | 69 | 40 | 58 | 16 | 81 | 00 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 21 | 84 | 22 | 28 | 26 | 46 | 66 | 16 | 36 | 66 |
| 86 | 17 | 43 | 49 | 85 | 40 | 51 | 40 | 10 | 46 |

